# **Iterated Reasoning with Mutual Information in Cooperative and Byzantine Decentralized Teaming**

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Figure 3. InfoPG enables iterated reasoning for robot decision-making.

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<u>4.</u> Alright,

and I will

<u>**3.**</u> Hmmm.

I better do

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## <u>Informational Policy Gradient (InfoPG)</u>: Algorithmic **Overview and Big-Picture**

- By assuming bounded-rational agents, we build a k-level, iterative architecture for InfoPG, inspired by the k-level reasoning from cognitive hierarchy theory.
- In InfoPG, each agent is equipped with an encoding and a communicative policy.



Figure 4. Decision rationalization in InfoPG.

- **InfoPG steps**: Depending on the decision-rationalization depth k...
- 1. At the beginning of a new rollout, each agent receives a state observation and produces an initial action  $\pi_{enc}^{i}(a^{i,(0)}|o^{i})$
- 2. Agents locally communicate their action guesses as high-dimensional latent distributions with neighboring agents
- 3. Agents repeat step #2 k times and update their action-guesses iteratively using their communicative policy  $\pi_{comm}^{i}(a^{i,(k)}|a^{i,(k-1)}, a^{j,(k-1)}, \dots, o^{i})$

### <u>InfoPG Variants</u>: Objective Function and Connection to Mutual Information (MI)

• Pursuant to the general Policy Gradient objective, we define the InfoPG objective as:

$$= \mathbf{E}_{\pi_{tot}^{i}} \left[ G_{t}^{i} \left( o_{t}^{i}, a_{t}^{i} \right) \sum_{j \in \Delta_{t}^{i}} \nabla_{\theta} \log \left( \pi_{tot}^{i} \left( a_{t}^{i, (K)} \middle| a_{t}^{i, (k-1)}, a_{t}^{j (k-1)}, \dots, o_{t}^{i} \right) \right) \right]$$

• Here  $G_t^i(o_t^i, a_t^i)$  represents the return. We propose two variants of InfoPG where:

$$G_t^i(o_t^i, a_t^i) = Q_t^i(o_t^i, a_t^i) \quad \text{s.t.} \quad Q_t^i(o_t^i, a_t^i) \ge 0$$
  

$$Or$$
  

$$G_t^i(o_t^i, a_t^i) = A_t^i(o_t^i, a_t^i) = Q_t^i(o_t^i, a_t^i) - V_t^i(o_t^i)$$
  

$$Adv. \text{ InfoPG}$$

• We derive a lower- and an upper-bound on the MI between agents' policy distributions:

$$I\left(\pi_{tot}^{i}\left(a^{i}\left|s^{i},a^{j}\right)\right) \leq I\left(\pi^{i};\pi^{j}\right) \leq 2\log(|A|) + 2\log\left(\pi_{tot}^{i}\left(a^{i}\left|s^{i},a^{j}\right)\right)\right)$$

- Depending on the sign of  $\nabla \pi_{tot}^i$ , the bounds of  $I(\pi^i; \pi^j)$  are "pushed" up or down • In InfoPG with the non-negative reward condition always pushes up the MI lower-bound • In Adv. InfoPG, the instantaneous sign of  $\nabla \pi_{tot}^i$  depends on the sign of  $A_t(o_t^i, a_t^i)$ • If  $A_t(o_t^i, a_t^i) > 0$  then the bounds of MI will shift  $\uparrow$ 
  - If  $A_t(o_t^i, a_t^i) < 0$  then the bounds of MI will shift  $\downarrow$

Adv. InfoPG modulates MI (rather than always maximizing it) depending on the cooperativity among agents and environment feedback.



- unreliable.



- Demo:

In summary, we show that not only InfoPG and Adv. InfoPG achieve higher cumulative results and better sample-efficiency than the baseline methods, but they also resulted in higher MI among agents, leading to a higher quality action coordination. • The Byzantine Generals Problem (BGP) Scenario: The BGP describes a scenario in which involved agents must achieve consensus on an optimal collaborative strategy without relying on a trusted central party, but where at least one agent is corrupt and disseminates false information or is otherwise

• We designed a BGP scenario in **Pistonball** where there is one "faulty" agent with untrainable random policy who the other

maximization, which uses a k-level theory of mind to deeply rationalize agents' action-decisions.

Results of InfoPG and Adv. InfoPG, in the BGP scenario show that always maximizing the MI may not always be desirable







Full-read:

